

Warmup

Determine the asymptotes for the graph

$$\text{of } f(x) = \frac{x}{x-1} \quad \text{HA: } y=1$$

$$x-1=0 \rightarrow \text{VA: } x=1$$

$$\text{Ex } f(x) = \frac{4x^2 + 6x - 37}{x+4} \quad \text{VA: } x=-4$$

HA: None

Slant asymptote

$$\text{Ex } f(x) = \frac{3x^2 - 2x + 2}{x-1} \quad \text{VA: } x=1$$

HA: None

$$\begin{array}{r} x-1 \overline{) 3x^2 - 2x + 2} \\ \underline{3x^2 - 3x} \\ 1x + 2 \\ \underline{1x - 1} \\ 3 \end{array}$$

$$\text{SA: } y=3x+1$$

Holes

When a numerator & denominator share a common factor.

$$\text{Ex } f(x) = \frac{\cancel{(x+2)}(x+3)}{x^2 \cancel{(x+2)}} = \frac{x+3}{x^2}$$

Hole @ $x=-2$

$$\text{VA: } x=0$$

$$\text{HA: } y=0$$